

1 Estimating dates of origin and end of COVID-19 epidemics

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6 Abstract

7 Estimating the date at which an epidemic started in a country and the date at which it can end
8 depending on interventions intensity are important to guide public health responses. Both are po-
9 tentially shaped by similar factors including stochasticity (due to small population sizes), super-
10 spreading events, and ~~memory-effects~~ memory effects (the fact that the occurrence of some events,
11 e.g. recovering from an infection, depend on the past, e.g. the number of days since the infection).
12 Focusing on COVID-19 epidemics, we develop and analyse mathematical models to explore how
13 these three factors may affect early and final epidemic dynamics. Regarding the date of origin, we
14 find limited effects on the mean estimates, but strong effects on their variances. Regarding the date
15 of extinction following ~~lock-down~~ lockdown onset, mean values decrease with stochasticity or with
16 the presence of superspreading events. These results underline the importance of accounting for
17 heterogeneity in infection history and transmission patterns to ~~make accurate predictions regarding~~
18 ~~epidemic temporal estimates~~ accurately capture early and late epidemic dynamics.

19 1 Introduction

20 The ability to make robust epidemiological inferences or predictions strongly relies on the law of large
21 numbers, which buffers the variability associated with individual processes. ~~Most~~ Many models of
22 infectious diseases spread are deterministic and therefore assume that the number of infected hosts is
23 large and above what has been termed the ‘outbreak threshold’ [12]. This assumption is violated at the
24 beginning and end of an epidemic, where stochasticity may have a strong effect [5].

25 In this study, we tackle two issues. First, we wish to estimate the date of origin of an epidemic in
26 a country, focusing on the case of COVID-19 outside China. This question is important because the
27 infection being imported, some cases may be detected before the reported beginning of an epidemic
28 wave, which is somehow counter-intuitive to an audience not familiar with stochasticity. ~~Conversely,~~
29 ~~cryptic transmission can take~~ Furthermore, transmission often takes place before an epidemic wave is
30 detected, as ~~observed thanks to~~ shown in several places using SARS-CoV-2 genomic data ~~in Washington~~
31 ~~state (USA) in Feb 2020 [3],~~ e.g. Washington state in the USA [3] or France [6]. Second, we investigate
32 how many days strict control measures need to last to ensure that the prevalence falls below key thresh-
33 olds. Despite its public health implications, this latter question has rarely been investigated. There are
34 some exceptions, for instance in the context of poliomyelitis [9], Ebola virus disease [26], and MERS
35 [21] epidemics, ~~but these~~. However, these estimates neglect superspreading events and/or do not
36 include non-Markovian effects (i.e. memory effects). Indeed, they often rely on ordinary differential
37 equations, meaning that the probability of an event to occur (e.g. recovering from an infection) does
38 not depend at all on the past (e.g. the number of days since the infection started). Recently, however,
39 it has been shown that incorporating secondary cases heterogeneity can significantly lower the delay
40 until an Ebola virus disease outbreak can be considered to be over [8].

41 Maintaining the lockdown so as to reach ‘zero-COVID’ requires extended effort because the incidence
42 might oscillate at a low value due to stochasticity for a long period. However, in practice, and as
43 illustrated by several countries, lockdown measures could be eased after the epidemic reaches a sufficiently
44 low incidence. Indeed, when the number of cases is low enough, stricter contact tracing, as well as local
45 control measures can be sufficient to stop the virus spread. For instance, in Taiwan or South Korea, the
46 epidemic was controlled for months as long as the incidence was kept below 20 new cases per day [18]
47 . In New Zealand, control measures were lifted only when the incidence reached 2 cases per day. This
48 is why we investigate the time for incidence to reach given thresholds that can be greater than 0.

49 The COVID-19 pandemic ~~has~~ led to an unprecedented publication rate of mathematical models,
50 several of which involve stochasticity. For instance, Hellewell *et al.* [14] analysed the initial steps
51 of the outbreak to estimate the fraction of the transmission chains that had to be tracked to control
52 the epidemics. Their results depend on the value of the basic reproduction number (denoted R_0),
53 which corresponds to the mean number of secondary infections caused by an infected individual in
54 an otherwise fully susceptible population [2], but also on individual heterogeneity. Indeed, if few
55 individuals tend to cause a large number of secondary infections while the majority tends to cause none,
56 the probability of outbreak emergence is much lower than if all individuals cause the same number of
57 secondary infections [17]. Accounting for this property, a study used the early COVID-19 outbreaks

58 incidence data in different countries to estimate the dispersion of the distribution of individual \mathcal{R}_0
59 R_0 [10]. Finally, Althouse *et al.* [1] have also used stochastic modelling to explore the role of super-
60 spreading events in the pandemic and its consequences on control measures.

61 Here, we develop an original discrete stochastic (DS) model, which features some of the known
62 characteristics of the COVID-19 epidemics. ~~In particular~~ The model is non-Markovian, which means
63 that individual histories matter for the dynamics. More specifically, the probability that an event
64 occurs (e.g. infecting another host) depends on the number of days spent in a state (e.g. being infected).
65 Furthermore, following earlier studies [14], we account for the fact that not all hosts transmit on the
66 same day post-infection. This is captured by assuming a distribution for the generation time, which is
67 the time between infection dates of an ‘infector’ and an infected person. Since the time of infection is
68 complicated to estimate, we approximate the generation time by the serial interval, which is the time
69 between the onset of the symptoms in the ‘infector’ and that in the infected person [19, 13]. We also
70 allow for heterogeneity in transmission patterns by assuming a negative binomial distribution of the
71 secondary cases. ~~Furthermore~~ To investigate the importance of stochasticity, we had to use deterministic
72 models in addition to ours. To have memory effects in a deterministic setting, we reanalysed an earlier
73 ~~deterministic~~ non-Markovian model [24] by setting the date of origin of the epidemic as the main free
74 parameter. Finally, to remove both memory effects and stochasticity, we analyse a classical determin-
75 istic Markovian model, which is commonly used to analyse COVID-19 epidemics [11]. ~~By comparing~~

76
77 By comparing the outputs of these models, we explore the importance of stochasticity, individual
78 heterogeneity, and non-Markovian effects on the estimates of the dates of origin and end of a nation-
79 wide COVID-19 epidemic, using France as a test case and mortality data because of its extensive sam-
80 pling compared to case incidence data.

81 2 Methods

82 2.1 The Discrete Stochastic (DS) model

83 Our model simulates the number of newly infected individuals per day (i.e. the daily incidence) as an
84 iterative sequence following a Poisson distribution. We assume that ~~each infected individual causes on~~
85 ~~average \mathcal{R}_0 secondary cases~~ the average number of secondary cases is equal to R_0 and that the host pop-
86 ulation is homogeneously mixed (i.e. no spatial structure), ~~an assumption that is~~. These assumptions
87 are relevant if a small fraction of the population is infected [27]. ~~We model the number of new infected~~
88 ~~individuals per day (i. e. the daily incidence) as an iterative sequence following a Poisson distribution.~~

89
90 More specifically, each individual is assumed to cause a random number of secondary infections
91 throughout his/her infection, depending on his/her infectiousness (β). Here, infectiousness represents
92 the relative infectious contact rate of an individual. It summarises both biological aspects (efficiency of
93 transmission per contact, susceptibility of the recipients), and the contact rate of the individual, during

94 the whole infectious period. Secondary infections occur randomly several days after contracting the
 95 disease. The probability of infecting someone some days after getting the disease is captured by the
 96 generation time, which we approximate using the serial interval [19].

97 Let $(Y_t)_{t \in \mathbb{N}}$ ω_a be a random variable describing the probability of infecting someone a days after
 98 contracting the disease. An individual infected since a days infects new individuals at a rate $R_0 \times \beta \times \omega_a$
 99 during that day. Therefore, the number of secondary infections occurring a days after being infected,
 100 which is considered as a count of independent events, follows a Poisson distribution parameterized by
 101 $R_0 \times \beta \times \omega_a$. From the additive property of the Poisson distribution, we find that the mean number of
 102 secondary cases during the entire infectious period is equal to the individual infectiousness. We then
 103 repeat this process for all individuals to determine the disease global progression.

Let Y_t be the random variable describing the incidence ~~over time~~, i.e. the number of new infections,
on day t , t being the number of days since initialisation of the process. For all $t \in \mathbb{N}$, the sequence of
 $(Y_{t+1})_{t \in \mathbb{N}}$ is such that The sequence of Y_{t+1} is defined using the Poisson additive property:

$$Y_{t+1} \sim \text{Poisson} \left(R_0 \eta_t \sum_{i=0}^t \omega_{t-i} \sum_{k=1}^{Y_i} F \beta_{k,i} \right) \quad (1)$$

104 where ~~ω_{t-i} is the probability of infecting someone at time t (i days after being infectious),~~ η_t is the
 105 average normalized contact rate in the population at day t , and ~~$F_{k,i}$ is the force of infection~~ $\beta_{k,i}$ is
 106 the infectiousness of individual k , infected at time day i . ~~The model is non-Markovian, which means~~
 107 ~~that individual histories matter for the dynamics. More specifically,~~ and ω_{t-i} is the probability of an
 108 individual infected at time i to infect someone at time t ($t - i$ is the probability that an event occurs
 109 (e.g. infecting another host) depends on the number of days spent in a state (e.g. being infected). Here,
 110 ~~these non-Markovian aspects are captured through ω , which is itself based on the generation time age~~
 111 ~~of the infection[19].).~~

112 We consider two scenarios (a) without and (b) with individual heterogeneity. If we denote by $\mathcal{F} \mathcal{B}$
 113 the distribution of random variables $(F_{x,y})_{(x,y) \in \mathbb{N}^2}$, where $F_{x,y}$ is the force of infection $\beta_{x,y}$ accounting
 114 for the infectiousness of an individual x infected at day y , then, in each scenario we assume that:

- a) \mathcal{F} is a Dirac distribution, noted $\delta(\mathcal{R}_0)$, implying that there is no heterogeneity and individuals
 have the same infectivity and infection duration distribution. The sequence $(Y_n)_{n \in \mathbb{N}}$ then simplifies
 into:-

$$\underline{Y_{t+1} \sim \text{Poisson} \left(\mathcal{R}_0 \eta_t \sum_{i=0}^t \omega_{t-i} Y_i \right)}$$

- 115 b) $\mathcal{F} \mathcal{B}$ is a Gamma distribution with shape parameter $k = 0.16$ and mean $\mathcal{R}_0 R_0$, implying that
 116 individuals are heterogeneous in infectivity-infectiousness and/or infection duration contact rate,
 117 which can lead to 'superspreading' events. We use the shape parameter (k) value estimated for a
 118 SARS outbreak in 2003 [17], which is consistent with early-estimates for SARS-CoV-2 epidemics
 119 [10, 1, 16, 25].

c) \mathcal{B} is a Dirac distribution, noted $\delta(1)$, implying that there is no heterogeneity and individuals have the same infectiousness and infection duration distribution. This is equivalent to $k \rightarrow +\infty$ in the previous scenario. The sequence $(Y_i)_{i \in \mathbb{N}}$ then simplifies into:

$$Y_{t+1} \sim \text{Poisson} \left(R_0 \eta_t \sum_{i=0}^t \omega_{t-i} Y_i \right) \quad (2)$$

To model the intensity of the control control intensity over the epidemic at time t such as, for instance, a national lock-down lockdown, we vary the contact rate parameter η_t . We assume that η_t is piecewise constant and that its discontinuities capture changes in public health policy policies (see Figure ??).

Overall, we define the temporal reproduction number ($\mathcal{R}R_t$) at time t such that

$$\mathcal{R}R_t = \eta_t \mathbb{E}[\mathcal{F}] \mathbb{E}[\mathcal{B}] = \eta_t \mathcal{R}R_0 \quad (3)$$

2.2 Beginning of the epidemic wave

To infer the starting date of the epidemic wave, we run our discrete stochastic (DS) algorithm starting from one infected individual until the infection dynamic becomes deterministic, *i.e.* the law of large numbers applies. We set the mortality incidence threshold to 100 daily deaths cases, which was reached on March 23 in France March 2020 in France. Neglecting the delay from infection to death, this would correspond to a daily incidence of more than 11,000 new cases according to the infection fatality ratio; a value much higher than the outbreak threshold above which a stochastic fade-out fade-out is unlikely [12]. We use independent estimates for the other parameters and perform a sensitivity analysis, shown in the Appendix.

To simulate death events in the DS model, we use the infection fatality ratio p and the delay from infection to death θ previously estimated on French data of ICU and deaths [24] (Table ??). These estimates compare very well with other independent estimates made from contact tracing data [15]. More specifically, if [28], *i.e.* the proportion of those infected who will go on to die from that infection. If we write X_t the number of individuals infected at time t who will die:

$$X_t \sim \text{Binomial}(Y_t, p) \quad (4)$$

We then chose For each of the X_t individuals, the day of death for each individual of X_t is set by drawing a time from infection to death following θ , *i.e.* a Gamma distribution. θ was previously estimated on French hospital data [24] (Table ??), and its estimate compare very well with other independent estimates made from contact tracing data [15].

We repeat the algorithm 10,000 times in-order to obtain a stable distribution of starting dates and discard epidemics that die out before reaching the threshold incidence.

139 To allow for comparison with empirical data, we ~~first smooth out week-end under-reporting by~~
140 ~~computing compute~~ a sliding average of this time series over a 7-days window.

141 Finally, we assume that the consequences of the ~~lock-down~~lockdown, which was initiated in France
142 on March 17, did not affect the death incidence time series until the very end of March because of the
143 delay between infection and death, which we estimate in France to be more than 11 days for 95% of the
144 cases [24].

145 2.3 End of the epidemic wave

146 ~~A national lock-down was established in France between Mar 17 and May 11, which drastically decreased~~
147 ~~the spread of the epidemic with an estimated efficacy of $1 - \eta_{FR} = 76\%$ [24]. On May 11, however, the~~
148 ~~virus was still circulating in France.~~

149 Here, we estimate how many additional days of ~~lock-down~~lockdown would have been necessary
150 to reach epidemic extinction for various ~~lock-down intensity post May 11.~~ ~~In the following we note~~
151 ~~by $(\zeta)_{t>55}$, the variation in the intensity of the lock-down after the 55 days of the official lock-down~~
152 ~~(i.e. after May lockdown intensity. Using the case of France as an example, the estimated lockdown~~
153 ~~contact rate is $\eta_{FR} = 0.243$, and we start our simulation on May 11), defined as-~~

$$\zeta_t = \frac{\eta_t - \eta_{FR}}{1 - \eta_{FR}}$$

154 where $\eta_{FR} = 0.24$ represents the estimated contact rate of the population during the first lock-down.

155 ~~, when the lockdown measures were partially lifted (i.e 55 days of lockdown).~~ To avoid the ~~unnecessary~~
156 accumulation of uncertainties, we initialise the model with incidence values obtained from a discrete-
157 time non-Markovian model [24] ~~on the period ranging from April 26 to May 11. This interval is chosen~~
158 ~~because most of the infections after May 11 originate from infections that started for the past 15 days~~
159 ~~before the start of the simulation, in France. This threshold arises directly from the choice of the serial~~
160 ~~interval distribution: 99.9% of the transmissions occur within less than 15 days ago (mathematically,~~
161 ~~$\mathbb{P}[w_i \leq 15] \leq 0.999$ using the model calibration for the serial interval $(w_i)_{i \in \mathbb{N}}$ in , using the generation~~
162 ~~time (Table ??).~~

163 We then use a Monte-Carlo procedure to estimate key features of the ~~sequence time series~~ $(Y_t)_t$,
164 such as the mean extinction time or the ~~asymptotic cumulative~~ extinction probability. This is done
165 by running 10,000 independent and identically distributed simulations of our process for each set of
166 parameters. ~~We stock each of these-~~

167 ~~We analyse the~~ 10,000 ~~trajectories and then analyse these trajectories as follow.~~ The scripts used for
168 ~~the simulations can be found in the supplementary materials.-~~

169 ~~resulting trajectories as follows.~~ First, we estimate the distribution of τ , which is the ~~minimal~~
170 ~~lock-down duration random variable corresponding to the minimal lockdown duration (in days) such~~

171 that the incidence is always null ~~afterwards for a given contact rate reduction post May 11. Mathematically,~~
 172 afterward for various scenarios. To mimic what happened during the first lockdown we set the contact
 173 rate to η_{FR} for the first 55 days. We then set the contact rate to a fixed value (greater or equal than η_{FR})
 174 until extinction is reached. As long as the effective reproductive number is lower than 1, the time to
 175 extinction is finite. Mathematically,

$$\tau = \inf_{s \in \mathbb{N}} \{Y_k = 0; \forall k \geq s\} \quad (5)$$

176 ~~The approximation of this distribution is obtained by assuming an infinitely long lock-down extension~~
 177 ~~under fixed contact reduction restrictions ($(\zeta_t)_{t>55} = \alpha$, with $0 \leq \alpha \leq 1$).~~

178 Second, we study the effect of finite ~~lock-down~~ lockdown extensions on the probability of extinc-
 179 tion ~~and focus on to understand~~ the risk of epidemic rebound upon ~~lock-down~~ lockdown lifting. For
 180 simplicity, we assume ~~no control (i.e. $\zeta_t = 1$) once the lock-down that control measures are completely~~
 181 lifted once the lockdown is over. The probability of having no new cases at time t ($p_0(t)$) is estimated
 182 using the following formula

$$p_0(t) = \frac{1}{N} \sum_{k=1}^N \mathbb{1}_{\{Y_t^k=0\}} \quad (6)$$

183 where N is the number of simulations performed and Y_t^k the number of newly infected individuals in
 184 the k -~~th~~ th simulation at time t .

185 Third, we study the effect of initiating the ~~lock-down~~ first lockdown one month or two weeks earlier
 186 ~~in the epidemic~~ (in France, on February 17 or March 03 respectively) on the distribution of the time
 187 to extinction (τ). For comparison purposes, we assume that ~~the spread of the dynamic is equal to~~
 188 ~~$\eta_{FR} = 0.24$ for in any case~~ the first 55 days of lockdown have the same contact rate ($\eta_{t \leq 55} = \eta_{FR}$) and then
 189 extend the ~~lock-down~~ lockdown indefinitely with variable intensities to estimate the time to extinction
 190 (τ) as described previously (see equation 5).

191 2.4 Alternative models

192 To further study the effects of stochasticity, non-Markovian dynamics, and superspreading, we imple-
 193 mented two ~~additional~~ deterministic models. The first is Markovian, i.e. memoryless, and is based on
 194 a simpler model derived from a classical SEIR model. The second has a discrete-time structure, which
 195 allows ~~to capture~~ capturing non-Markovian dynamics [24].

196 The SEAIRHD model

197 In this classical compartment model, hosts can belong to seven states: susceptible to infection (S),
198 exposed (i.e. infected but not infectious, E), asymptomatic and infectious (A), infectious and symp-
199 tomatic (I), removed (i.e. recovered or isolated, R), hospitalised who will die (H), or dead (D) (Fig. ??).
200 The model is described by a set of ODE detailed in the ~~appendix. In the simulations, we assume~~
201 ~~that one exposed individual starts the epidemic~~ Appendix (equation system ??). Since the model is
202 deterministic, we can seed the simulations with a single exposed individual on day t_0 .

203 This model is solved numerically using the Numpy package ~~on in~~ Python 3.8.3 to obtain a deter-
204 ministic trajectory ~~with the parameters fitted to the empirical data, with a moving average of 7 days.~~
205 Parameters were chosen with maximal likelihood given the observed daily mortality data, assuming
206 that the daily mortality incidence is Poisson distributed, and independence between daily incidences
207 (For more details, see the supplementary material). We also simulate a stochastic version of this model
208 1,000 times using a Gillespie algorithm with the package TIPS [7] in R v.3.6.3 [23].

209 COVIDSIM: A non-Markovian deterministic model

210 ~~We estimate dates of origin and end of epidemics using~~ Finally, we use an existing discrete-time model
211 that has a similar structure to the continuous model mentioned above with an additional age-structure
212 [24]. ~~The serial interval is~~ For comparison purposes, the generation time is set to be the same as in
213 our DS model [20], and so ~~is the use of the~~ (non-exponential ~~delays~~ delay) from infection to death.
214 However, two major differences are that this ~~earlier~~ third model is not stochastic and does not allow
215 for superspreading events. We restricted the parameter inference to the daily ~~death~~ hospital mortality
216 data described previously, with the main free parameter being the date of origin. We invite the reader
217 to refer to [24] for the scripts and further details on this approach.

218 2.5 Model calibration

219 To allow for model comparison and improve estimates, we ~~fixed~~ fix some key parameters based on
220 existing values, focusing on the French COVID-19 epidemic. Table ?? lists all the parameters used
221 along with key references.

222 ~~The~~ We compute the likelihood of the deterministic SEAIRHD model ~~was computed~~ assuming a
223 Poisson distribution of the daily mortality incidence data. Parameter inference with maximum like-
224 lihood ~~was~~ is performed using the Powell-Nelder-Mead algorithm implemented by Scipy.minimize
225 function in Python.

226 The parameters used for the non-Markovian deterministic model correspond to the maximum
227 likelihood set of parameters used in [24].

228 2.6 [Code and simulation results](#) availability

229 The different scripts [and simulation results](#) are available on Gitlab:

230 <https://gitlab.in2p3.fr/ete/origin-end-covid-19-epidemics>

231 3 Results

232 3.1 Origin of the epidemic wave

233 When neglecting host heterogeneity, using our DS [algorithm framework](#), the median delay between the
234 importation of the first case of the epidemic wave and the time mortality incidence reaches 100 deaths
235 per day ([March 23](#)) is 67 days (equivalent to a first case on January 16 in France), with a 95% confidence
236 interval (95% CI) between 62 and 79 days, *i.e.* between January 4 and 21 in France (Fig. 1). With this
237 model, only 7% of the outbreaks die out before reaching the threshold.

238 Superspreading events, *i.e.* when the individual ~~force of infection \mathcal{F}~~ [infectiousness \$\mathcal{B}\$](#) follows a
239 Gamma distribution, seem to have limited effects on these results: the median delay drops slightly to
240 64 days (January 19 in France), although with a larger 95% CI, between 54 and 85 days. Moreover, as
241 expected [17], we observe a soar in the frequency of epidemic outbreaks dying out before reaching the
242 threshold, which represent 75% of our simulations.

243 When assuming ~~a deterministic Markovian~~ [deterministic and Markovian dynamics with our](#) SEAIRHD
244 model, the ~~date of importation~~ [importation date](#) of the first case of the epidemic wave that best fits the
245 results is ~~slightly later than the DS models estimates~~ [similar](#), with a delay of 63 days until daily mor-
246 tality incidence reaches 100 ~~deaths~~ [cases](#). A stochastic implementation of the same model yields the
247 same median delay of 63 days ~~, and a~~ [95% ~~confidence interval between~~ [CI](#): 56 ~~and~~ [76](#) days], which
248 is comparable to the DS model. However, consistently with earlier studies [24, 11], the ability of this
249 memoryless model to capture the data is limited (Fig. ?? in the Appendix). Finally, the maximum likeli-
250 hood parameter estimates from a deterministic ~~but~~ non-Markovian model, [COVIDSIM](#) [24], restricted
251 to the mortality data, indicates a similar delay of 63 days (January 20), ~~with a~~ [95% ~~CI between~~ [CI](#): 63 ~~and~~
252 [64](#) days].

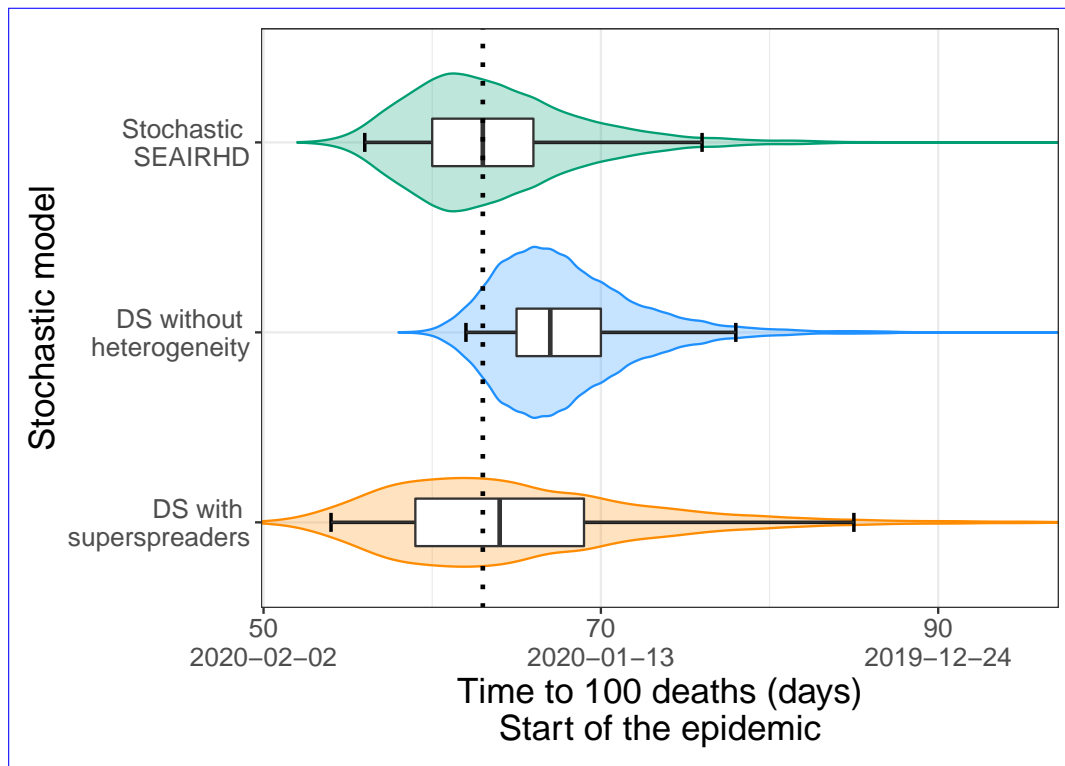


Figure 1 – ~~Estimated distribution of the number of days until daily mortality incidence reaches 100 deaths.~~ Estimated distribution of the number of days until daily mortality incidence reaches 100 cases. The boxplots and the whiskers indicate the 2.5%, 25%, 50%, 75%, and 97.5% quantiles out of the 10,000 simulations. The red dashed line shows the estimates using the deterministic models.

253 We perform a sensitivity analysis of our results focusing on two ~~of our~~ parameters. First, we show
 254 that the median delay for daily ~~incidence mortality~~ to reach 100 ~~deaths is decreased~~ cases is increased
 255 by 5 days when the ~~serial interval generation time~~ standard deviation is decreased by one third (Fig. ??).
 256 ~~Those estimates therefore~~ Therefore, the estimates remain within the confidence interval ~~of our starting~~
 257 ~~date obtained for the starting date of the epidemic~~. Second, increasing the number of initially imported
 258 cases from 1 to 5 decreases the delay by ~~8 days~~ 7 days, with a median of 60 days [95% CI: 57-64 days]
 259 without heterogeneity. However, when assuming a more realistic scenario where all those cases are not
 260 imported on the same day, ~~we find a much more limited impact on the delay~~ this impact of the delay
 261 was more limited (Fig. ??). For example, if the 5 cases are imported during the first five days of the
 262 outbreak, the decrease is only of 5 days, with a median delay of 62 days [95% CI: 59 - 66 days].

263 Overall, non-Markovian dynamics or stochasticity do not tend to ~~significantly~~ strongly impact the
 264 estimate of the delay for an epidemic to reach a daily mortality incidence of 100 ~~deaths~~ cases. Introduc-
 265 ing super-spreading events, however, slightly decreases the delay estimated and greatly increases its
 266 variance. As expected, the initial number of imported cases can have an impact on the estimates.

267 3.2 End of the epidemic wave with ~~lock-down~~lockdown

268 Time to eradication

269 We ~~estimated~~estimate the distribution of the minimal ~~lock-down~~lockdown duration to eradicate the
270 epidemic (τ). ~~We first neglect by first neglecting~~ superspreading events and ~~start~~starting from the
271 end of the first-wave ~~lock-down~~lockdown in France on May 11 (orange violins in Figure 2). When
272 maintaining the constraints on social interactions to their full intensity ($\zeta_{t>55} = 0, \eta_{t>55} = 0.24$), a total
273 of at least ~~7.6 months of lock-down~~8 months of lockdown, including the 55 days between Mar 17 and
274 May 11, are required to reach a ~~95~~97.5% extinction probability.

275 When accounting for individuals heterogeneity, we find that, everything else being equal, the quan-
276 tiles of the time to eradication (τ) are always lower than ~~in homogeneous case~~the homogeneous cases.
277 However, ~~6.9 months of lock-down~~7.23 months of lockdown at full intensity ($\zeta_{t>55} = 0, \eta_{t>55} = 0.24$) are
278 still required to guarantee ~~95% chance of extinction~~extinction in 97.5% of the cases (blue violins in Fig-
279 ure 2). ~~Here, taking into account the individual heterogeneity~~Accounting for individual heterogeneity
280 ~~also~~ reduces the variance of τ . ~~Indeed, transmission heterogeneity implies that~~This is expected because
281 ~~in this case~~, the majority of the infected people do not transmit, which increases the extinction proba-
282 bility [17].

283 The mean values of the time to eradication (τ) increases with the decrease in the intensity of the
284 ~~lock-down constraints ($\zeta_{t>55}$)~~. As ζ_t tends towards $\frac{1-\eta_{FR} R_0}{(1-\eta_{FR}) R_0}$ ~~lockdown constraints post 55 first days~~
285 ~~of lockdown~~. As the contact rate of the population tends towards $1/R_0$ the mean values of τ diverge
286 towards infinity. The dynamical process is said to be critical (resp. super-critical) if $\eta_t = \frac{1}{R_0} \eta_t = 1/R_0$
287 (resp. $\eta_t \geq \frac{1}{R_0} \eta_t \geq 1/R_0$). This result holds ~~true~~ when assuming transmission heterogeneity.

288 We also compute the time to extinction with the deterministic SEAIRHD model after tuning the
289 model using the parameters that best fitted the mortality incidence (Fig. 2). The time to extinction
290 corresponds here to the minimum time where the incidence reaches zero.

291 Rebound risk

292 In our stochastic model, ~~a newly infected individual may cause several secondary infections δ days~~
293 ~~after being infectious~~. Therefore, the incidence at time t (denoted $(Y_t)_{t \in \mathbb{N}}$) can alternate between zero
294 and non-zero values. To evaluate the risk of epidemic rebound, we implement a finite ~~lock-down~~
295 ~~lockdown~~ extension after which all constraints are released ($\eta_t = 1 \Leftrightarrow \zeta_t = 1, \eta_t = 1$). This allows us to
296 calculate $p_0(t)$, the probability to have 0 new cases after time t . In Figure ??, we see a sharp decrease in
297 $p_0(t)$ a few days after ~~lock-down~~lockdown release.

298 The rebound risk is directly linked to the ~~random variable ($F_{x,y}$) (the force of infection of an individual~~
299 ~~x infected y days after the start of the simulation)~~. Assuming transmission heterogeneity. Assuming a
300 higher individual transmission heterogeneity (i.e. lower k) drastically reduces the risk of rebound, as it
301 also implies that most infectees do not transmit the disease.

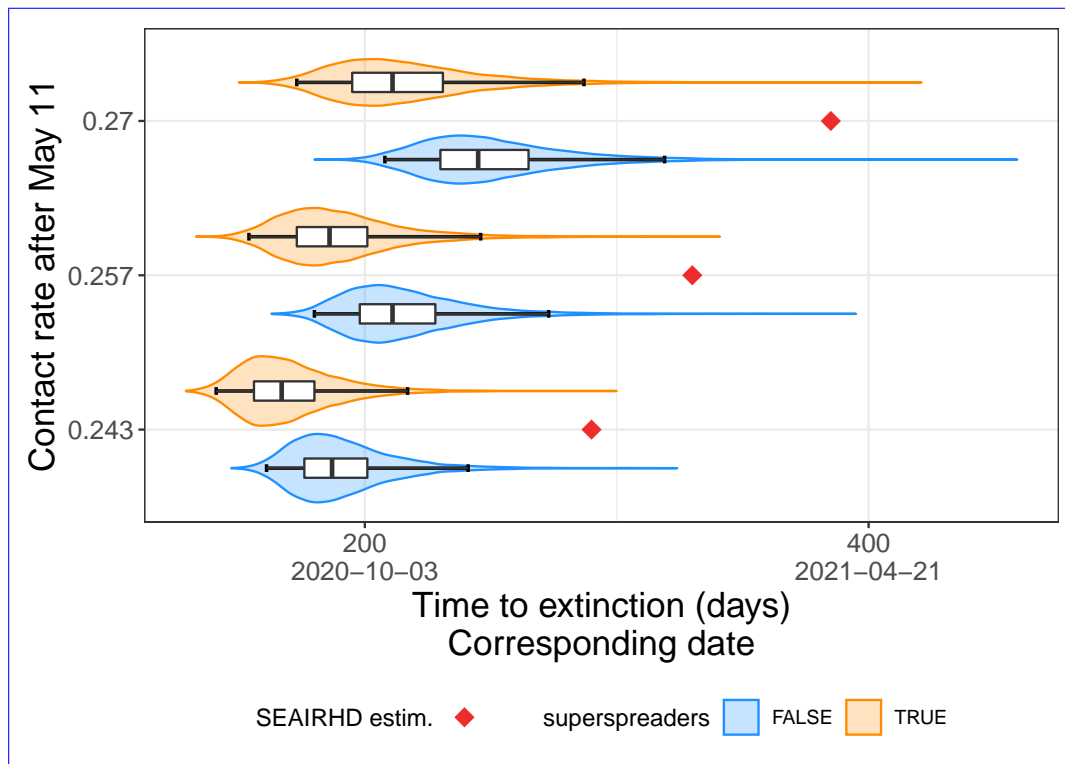


Figure 2 – **Effect of the lock-down intensity, stochasticity, and superspreading events on the time to extinction (τ).** The distributions of τ (number of in days since the start of the lockdown on Mar March 17) for several lockdown intensities increase (η_L) after the first 55 days (i.e. after May-11 May 2020) are plotted on the Y-axis (ζ) using violin plots and boxplots. Results without transmission heterogeneity ($\mathcal{F} = \delta(R_0), \mathcal{B} = \delta(R_0)$) are in orange. In blue, we assume a Gamma distribution for \mathcal{F}, \mathcal{B} . Red diamonds show results from the deterministic Markovian model. The box extends from the lower to upper quartiles of the data. The whiskers expand from the 2.5% to the 97.5% quantiles.

302 Eradication and lockdown initiation date

303 We now turn to the consequence of implementing a lockdown a month or two weeks earlier.
 304 In France, this corresponds to Feb 17 and Mar 03 (at that time, a total of respectively 1 and 3 deaths were
 305 reported).

306 The results are shown in Figures ?? Figure ?? for the case without host heterogeneity and Fig. ??
 307 3 with superspreading events. Initiating the lockdown one month earlier, i.e. for France
 308 approximately 33 days after the onset of the epidemic wave, decreases the 95/97.5% quantile of τ by
 309 96 days without the time to extinction by 91 days with transmission heterogeneity (92 days with 97
 310 days without heterogeneity) in the most restrictive scenario. If the onset of the lockdown is
 311 brought forward by two weeks (Mar 03 March 3rd), i.e. in France approximately 48 days after the onset
 312 of the epidemic, 95/97.5% of the extinction events occur before the 188th days of lockdown without 178th
 313 day of lockdown with transmission heterogeneity (169th days with 199th day without heterogeneity).

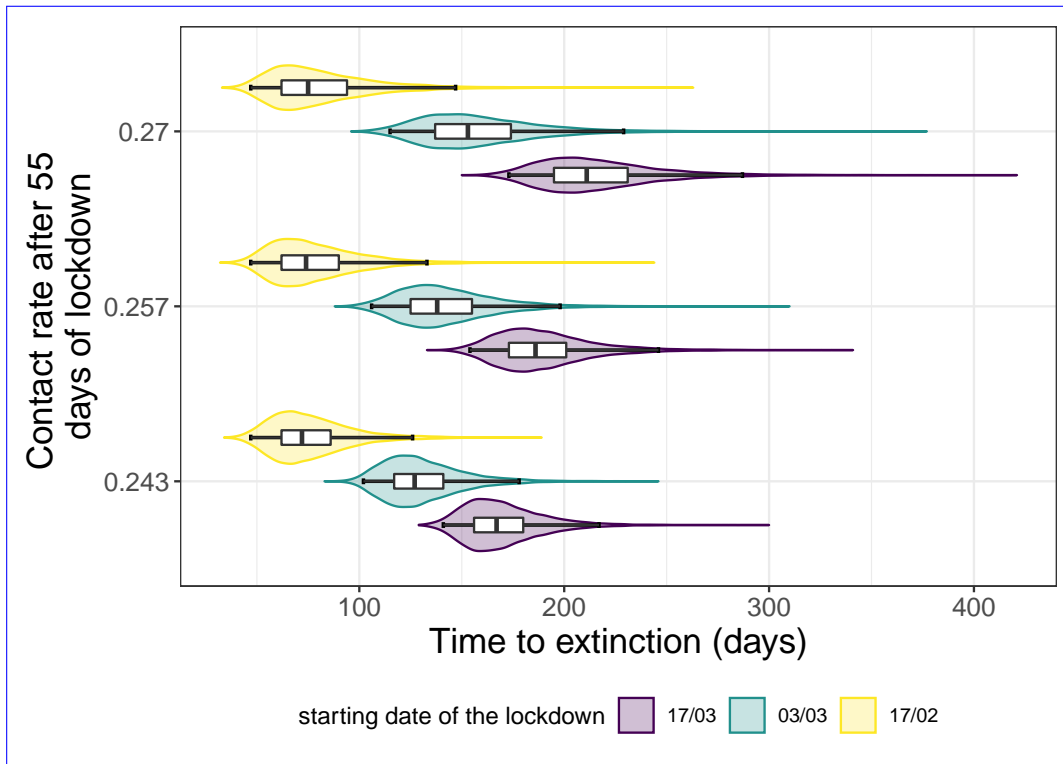


Figure 3 – Effect of the lockdown intensity, stochasticity, and initiation date on the time to extinction (τ) under individual spreading heterogeneity assumption. The distributions of the time to extinction (in days since the start of the lockdown) for several contact rate restrictions post 55 first days are plotted on the Y-axis using violin plots and boxplots. In this graph, we assume individual spreading heterogeneity. The colors indicate the different initiation date of the lockdown: in purple it starts on Feb 17, green Mar 03, and yellow on Mar 17 (official start). The box extends from the lower to upper quartiles of the data. The whiskers expand from the 2.5% to the 97.5% quantiles.

314 Hence a reduction of 41-39 (resp. 38-42) days of lock-down-lockdown could be expected compared to
 315 the later-actual start (Mar 17).

316 These numbers increase with the easing of the constraints following the first 55 days of strict lock-down
 317 (η_{FR} lockdown ($\eta_t = 0.24$)). When assuming a lighter control in the following days (e.g. $\zeta_{t>55} = 6.6\%$ $\eta_{t>55} = 0.29$),
 318 one can notice that the increase in the quantiles of τ when starting the lock-down-lockdown on Feb 17
 319 is much lower than the two other cases. Since the epidemic has not spread to same extent in the latter
 320 scenario,

321 Time to a threshold of 20 new cases per day

322 Finally, we study the distribution of the delay to reach 20 new cases per day, below which it is expected
 323 that a general lockdown is not required to control the epidemic. We evaluate the effect of lockdown
 324 intensity, initiation date and individual spreading heterogeneity on this delay.

325 The estimated distributions of the time to 20 new daily cases when accounting for superspreading

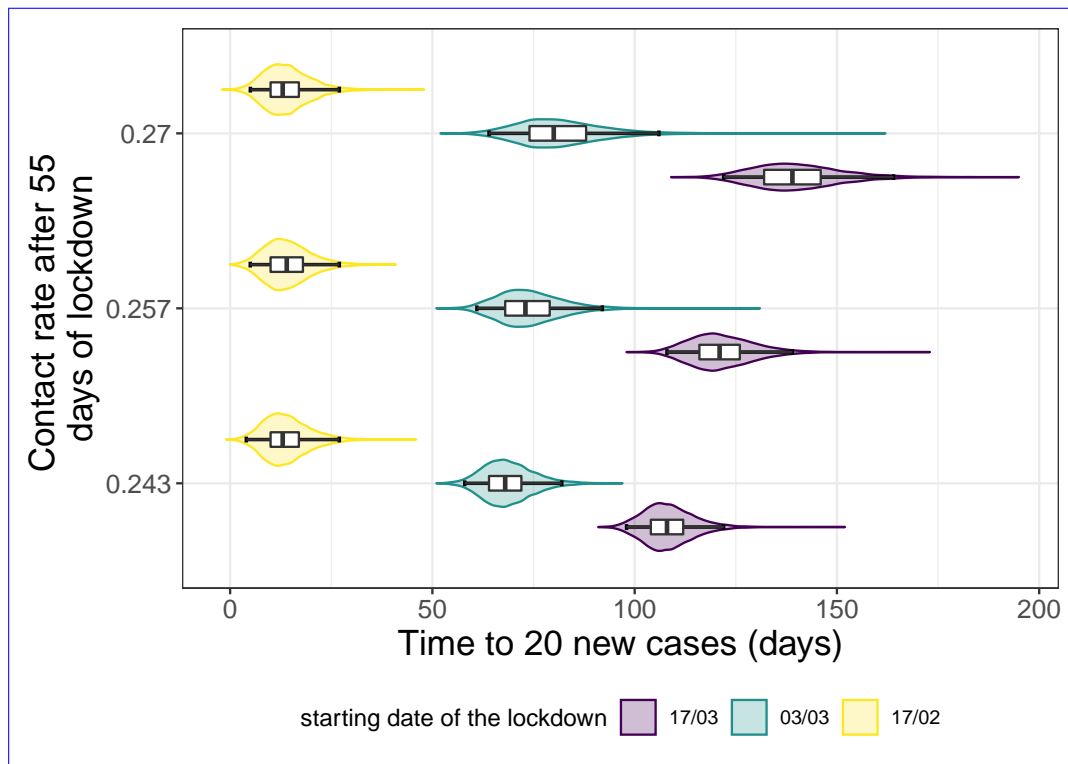


Figure 4 – **Effect of the lock-down intensity, stochasticity, and initiation date on the time to extinction (τ) without superspreading events.** **Effect of the lockdown intensity, stochasticity, and initiation date on the time to 20 new cases under individual spreading heterogeneity assumption.** The distributions of τ – the time to 20 new cases (number of in days since the start of the lock-down on Mar 17 lockdown) for several lock-down intensities increase after the first contact rate restrictions post 55 first days are plotted on the Y-axis (ζ) using violin plots and boxplots. In this graph we assume there is no individual spreading heterogeneity. The colors indicate the different initiation date of the lock-down lockdown: in purple it starts on Feb 17, green Mar 03 and yellow on Mar 17 (official start). The box extends from the lower to upper quartiles of the data. The whiskers expand from the 2.5% to the 97.5% quantiles.

326 events is displayed in Figure 4 (see Figure ?? for the estimations without superspreaders). Our model
 327 suggests that initiating control measures one month earlier (mid-February) would have reduced the
 328 97.5% quantile of the time to 20 new cases by 95 days under the strictest restrictions. In the mid-February
 329 scenario, we notice the time to 20 new cases occurs during the 55 first days of lockdown. Starting the
 330 lockdown early March does reduce the 97.5% quantile of the time to the threshold by 40 days. However,
 331 the first 55 days of lock-down are decisive in the slow-down of the epidemic lockdown are not sufficient
 332 to reach the limit of 20 new cases per day.

333 4 Discussion

334 In the early and final stages of an epidemic, stochastic forces may strongly affect transmission dynamics
 335 because infection prevalence is low. Using stochastic mathematical modelling, and assuming $R_0 = 3$,

336 we estimate the time for a COVID-19 epidemic to reach an incidence of 100 deaths per day to be ap-
337 proximately 67 days, with a 95% probability between 62 and 79 days. In the case of France, where such
338 incidence values were reached on Mar 23, this translates into an origin of the ~~first~~ epidemic around
339 January 16, with 95% probability between January 4 and 21. This is consistent with estimates obtained
340 using virus genome data, although these should be interpreted with caution due to the uncertainties
341 regarding the molecular clock estimates for the virus and the incomplete sampling in France [6].

342 Accounting for superspreading events ~~does yield~~ yields a later median date of origin (January 19 for
343 France). This ~~faster dynamic comes from the fact that simulated~~ is expected because, in outbreaks that
344 do not die out ~~(and therefore are accounted in the results)~~ are mostly due to early superspreading events
345 ~~, which can lead to a faster initial dynamic,~~ superspreading events accelerate the initial dynamics [17].
346 However, this difference is not significant.

347 ~~In general, the~~ The 95% ~~confidence intervals~~ CI for the epidemic starting date generated by our
348 different models overlap. This could originate from our use of mortality data. Since death occurs after
349 a mean delay of 23 days after infection [24], by the time ~~incidence starts to increase~~ mortality incidence
350 is detectable, transmission dynamics are largely deterministic. This also explains why introducing
351 superspreading events mostly ~~increases the origin date uncertainty~~ affects the variance of the estimate.
352 Unfortunately, hospital admission ~~date~~ data is not available for France until ~~Mar-18~~ March 2020, and
353 screening data was initially performed with a very low sampling rate in the country (only severe cases
354 were tested).

355 Care must be taken when comparing the estimates from our discrete stochastic model to that of
356 earlier models. For instance, the non-Markovian deterministic ~~model by Sofonea et al.~~ COVIDSIM
357 model [24], which estimates the date of onset to be slightly later (January 20), includes host age struc-
358 ture. Regarding the more classical deterministic and Markovian SEAIRHD model, its ability to fit the
359 data is limited (Fig. ??), except when only considering the exponential phase before the lockdown. This
360 poor inference of underlying epidemiological dynamics is ~~largely likely~~ due to the absence of memory
361 in the underlying processes, as stressed by earlier studies [24, 11]. When incorporating memory on
362 the ~~hospitalization to death~~ hospitalization-to-death delay, we obtain a much better fit, and the time
363 to ~~100 daily deaths~~ the daily mortality of 100 cases is then comparable to that of the model without
364 superspreading events.

365 We also ~~estimated the mean~~ estimate the median number of days of full intensity ~~lock-down~~ lockdown
366 required to achieve extinction with a 95% confidence. ~~With our stochastic model~~ In the French setting
367 (i.e. introduction of the lockdown after 67 days of the epidemic), we find ~~that in average 190~~ (IC
368 with our stochastic model that 187 (95% :-183-199CI: [161, 241]) days of ~~lock-down are necessary~~
369 lockdown would be required to reach extinction in a homogeneous ~~scenario, starting the lock-down~~
370 mid-March transmission scenario in 50% of the cases. Accounting for superspreading events decreases
371 the median estimate value by 20 days. Initiating the ~~lock-down~~ lockdown one month earlier strongly
372 affects these estimates: a 30 days anticipated start reduces the mean number of days spent in full inten-
373 sity ~~lock-down by 96~~ lockdown by 95 days, i.e. a ~~49~~ 51% reduction.

374 50% of the simulations reach the threshold of 20 new cases after 108 (95% CI: [98, 122]) days of

375 ~~lockdown at full intensity initiated mid-March. When initiating the constraint in mid-February, this~~
376 ~~threshold is reached in 13 (95% CI: [4, 27]) days. Since, in the latter scenario, the epidemic spread is~~
377 ~~more limited, the first 55 days of lockdown are decisive in the slowing down of the epidemic.~~ This
378 confirms that early interventions have a disproportionate impact ~~on the epidemic dynamic.~~

379 Finally, we investigated the risk of an epidemic rebound upon ~~lock-down~~ ~~lockdown~~ lifting. In this
380 scenario, super-spreading has a striking impact ~~as-expected~~ in limiting this risk, ~~which is consistent~~
381 ~~with earlier work on outbreak emergence [17].~~

382 There are several limitations to this work. First, the ~~serial interval~~ ~~generation time~~ ω and the time
383 from infection to death θ , ~~are-remain~~ largely unknown in France, as well as in many countries. Most
384 ~~of the known~~ serial interval estimates rely on contact tracing data from Asia [16, 19], which could ~~be~~
385 ~~slightly-different~~ ~~differ~~ from the distribution in France, due to ~~different~~ ~~differences in~~ contact structure,
386 or ~~different~~ non-pharmaceutical ~~measures applied.~~ ~~Obviously, the serial interval distribution has a~~
387 ~~strong impact on the dynamics. We do show however~~ ~~interventions.~~ ~~Although the generation time~~
388 ~~distribution is expected to affect epidemic dynamics, we show~~ in Figure ?? that the variance of this
389 interval ~~does not have a strong impact on the~~ ~~has little impact on our~~ results.

390 Another important limitation about the estimation of the date of origin of the epidemic comes from
391 the assumption that only ~~one initial~~ ~~a single~~ infected person caused the epidemic. ~~Clearly, most~~ ~~Most~~
392 epidemics outside China were seeded by multiple importation events. The problem is that there is an
393 identifiability issue because it is impossible to estimate both the number of initial infected cases and
394 the time to ~~a~~ threshold of 100 deaths with incidence data only. However, some estimates made in the
395 UK from phylogenetic data as well as the combination of prevalence and travel data show that the
396 estimated number of importation events is less than 5 per day before the end of February, when the
397 virus was beginning to circulate at higher levels throughout Europe [22]. Assuming ~~that the dynamic~~
398 ~~was similar~~ ~~a similar importation pattern~~ in France, we ~~could verify~~ ~~show~~ that the dynamic ~~was is~~
399 only sensitive to the importation events within the first days after the beginning of the epidemic wave.
400 While these events may have ~~enabled~~ ~~helped~~ the epidemic to escape the stochastic phase faster, they
401 ~~would not have strongly affected~~ ~~are unlikely to strongly affect~~ the estimated date of ~~the~~ beginning of
402 the wave (Figure ??). In a quite extreme scenario of 5 importations per day during 30 days, ~~we estimate~~
403 the median day of the epidemic beginning ~~was estimated~~ to be 16 days later (*i.e.* Feb 2 for France).

404 Another limitation comes from the lack of data regarding individual heterogeneity in COVID-19
405 epidemics. Such heterogeneity was supported by early limited data [10, 16] but recent additional ev-
406 idence from Chinese transmission chains further supports this result [25], although with a higher k
407 parameter value ~~that than~~ the one used here (0.30 versus 0.16 here), meaning a less heterogeneous
408 transmission. Therefore, our assessment of superspreading events impact seems conservative.

409 These results have several implications. First, they can help reconcile the fact that cases may be
410 detected long before the emergence of the transmission chains related to an epidemic wave. This is
411 particularly important for an audience not familiar with stochasticity. Second, the estimate of the time
412 required to ensure that the epidemic is gone ~~is directly informative to public health officials~~ ~~can help~~
413 ~~inform public health decisions.~~ In the case of ~~France~~ ~~the French epidemic~~, for instance, ~~one can directly~~

414 ~~see that~~ enforcing a strict ~~lock-down~~lockdown from March 17 until epidemic extinction ~~is~~was prac-
415 tically unfeasible. ~~This~~However, this may not be the case if measures are taken early enough in the
416 epidemic. Furthermore, our work also illustrates the risk of epidemic rebound as a function of the du-
417 ration of the ~~lock-down~~lockdown. Overall, this work calls for further studies, especially to assess the
418 importance of super-spreading events in the global spread of SARS-CoV-2.

419 Acknowledgements

420 Thomas Beneteau is supported by a doctoral grant from the Ligue Contre le Cancer. We thank the
421 CNRS, the IRD, and the IRD itrop HPC (South Green Platform) at IRD montpellier for providing HPC
422 resources that have contributed to the research results reported within this paper. We also thank the
423 ETE modelling team for discussion.

424 This article was submitted on medRxiv [4].

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